



Supporting Calculations in KS2





What we'll look at...

- When do we first learn written methods for $+$, $-$, \times and \div ?
- What is the key vocabulary to use?
- Using visual representations to help understand the written method.
- Expectations for end of Year 6.



Addition...

- Written method first appears in Year 3.

Add two numbers (no exchange)

Mental strategies and introduction of formal written method.

... ones + ... ones = ... ones
... tens + ... tens = ... tens
... hundreds + ... hundreds = ... hundreds

Hundreds	Tens	Ones
100 100 100	10 10 10 10	1 1 1 1 1
100 100 100 100	10 10 10	1 1

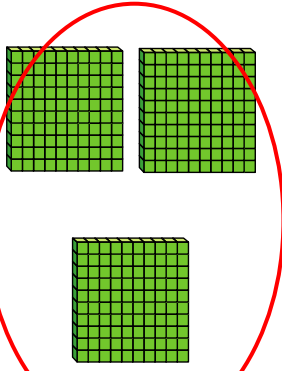
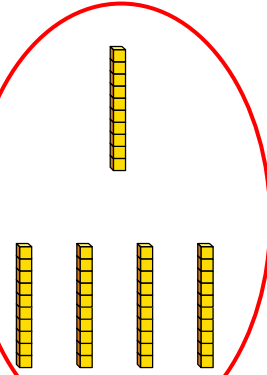
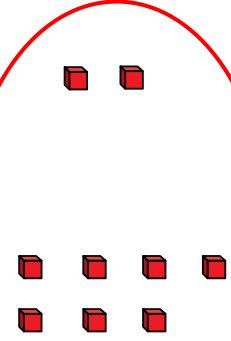
?	
345	432

H	T	O
3	4	5
+		
4	3	2



Addition...

$$212 + 147 = 359$$

	Hundreds	Tens	Ones
			
+			
	3	5	9

	H	T	O	
	2	1	2	
+	1	4	7	
	3	5	9	

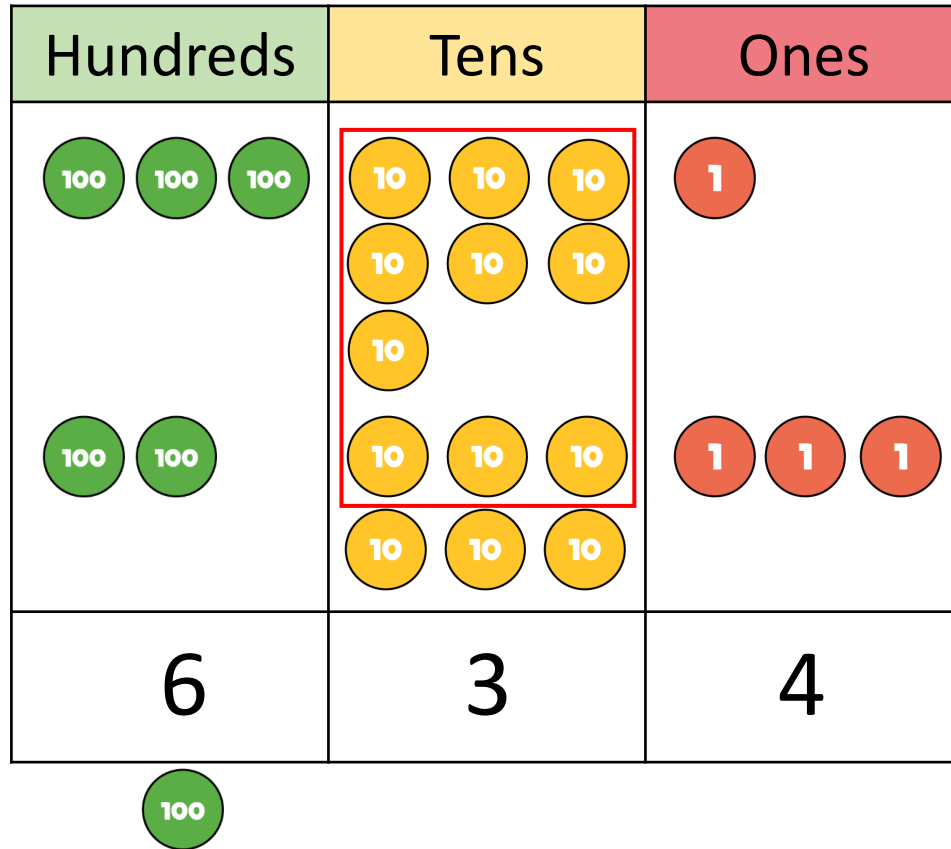
Do we have enough hundreds to make an exchange?



Addition...

Dexter scores 371 points in a game.
Rosie scores 263 points.

How much do they score altogether? **634**

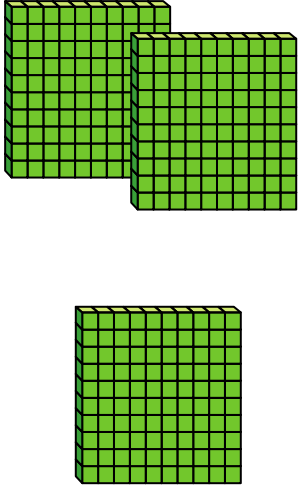
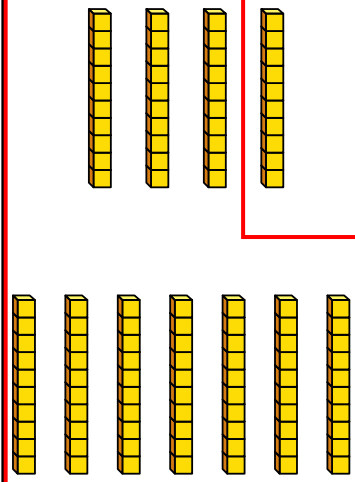



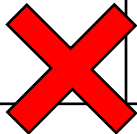
	H	T	O	
	3	7	1	
+	2	6	3	
	6	3	4	
	1			

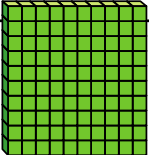


Addition...

$$243 + 172 = 415$$

Hundreds	Tens	Ones
		
4	11	5



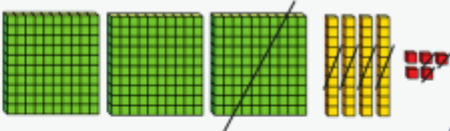
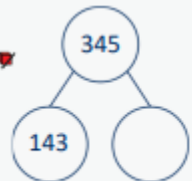
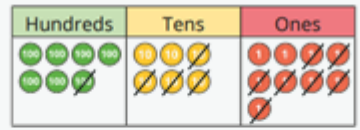
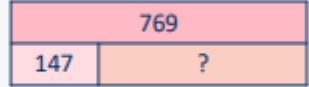



	H	T	O	
	2	4	3	
+	1	7	2	
	4	1	5	
	1			



Subtraction...

- Written method first appears in Year 3.

<p>Subtract two numbers (no exchange)</p> <p>Mental strategies and introduction of formal written method.</p>	<p>... ones – ... ones = ... ones ... tens – ... tens = ... tens ... hundreds – ... hundreds = ... hundreds</p>     
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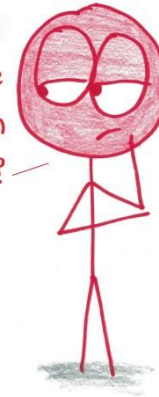
Subtraction...

$$\begin{array}{r} 6 \quad 16 \\ 76 \\ -19 \\ \hline 57 \end{array}$$

I borrowed
a ten!



Really? You
plan to give
it back when
you finish?



$$\begin{array}{r} 6 \quad 16 \\ 76 \\ -19 \\ \hline 57 \end{array}$$

Well... no....



In that case,
can I borrow
\$20 and some
chocolate?

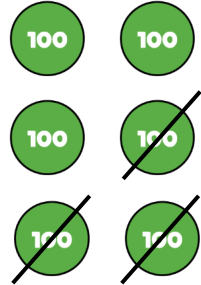
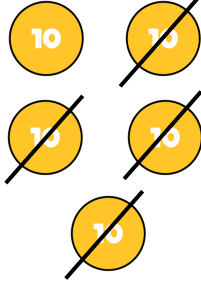
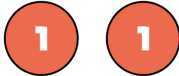




Subtraction...

Have a think 

$$652 - 340 = 312$$

Hundreds	Tens	Ones
		
3	1	2

	H	T	O	
	6	5	2	
-	3	4	0	
	3	1	2	

Do we need to make an exchange?



Subtraction...

Have a think

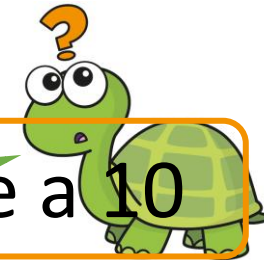


$$451 - 325 =$$

	H	T	O
	4	5	1
-	3	2	5

Q Will just subtract each digit from one?

No, you need to exchange a 10



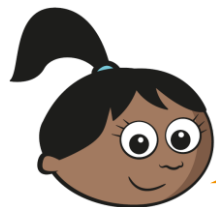


Subtraction...

$$451 - 325 = 126$$

Hundreds	Tens	Ones
1	2	6

	H	T	O	
	4	5 ⁴	¹ 1	
-	3	2	5	
	1	2	6	



I will exchange 1 ten for 10 ones.



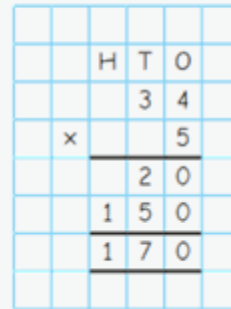
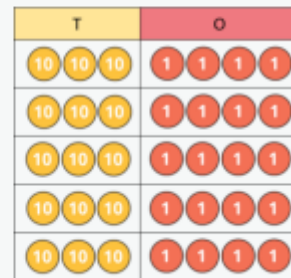
Multiplication...

- Written method first appears in Year 4.

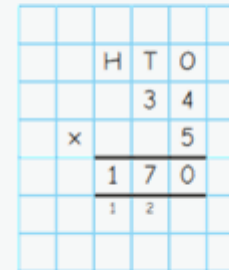
Multiply a 2 or 3-digit number by a 1-digit number

The short multiplication method is introduced for the first time, initially in an expanded form.

To multiply a 2-digit number by ... , I multiply the ones by ... and the tens by ...
To multiply a 3-digit number by ... , I multiply the ones by ... , the tens by ... and the hundreds by ...



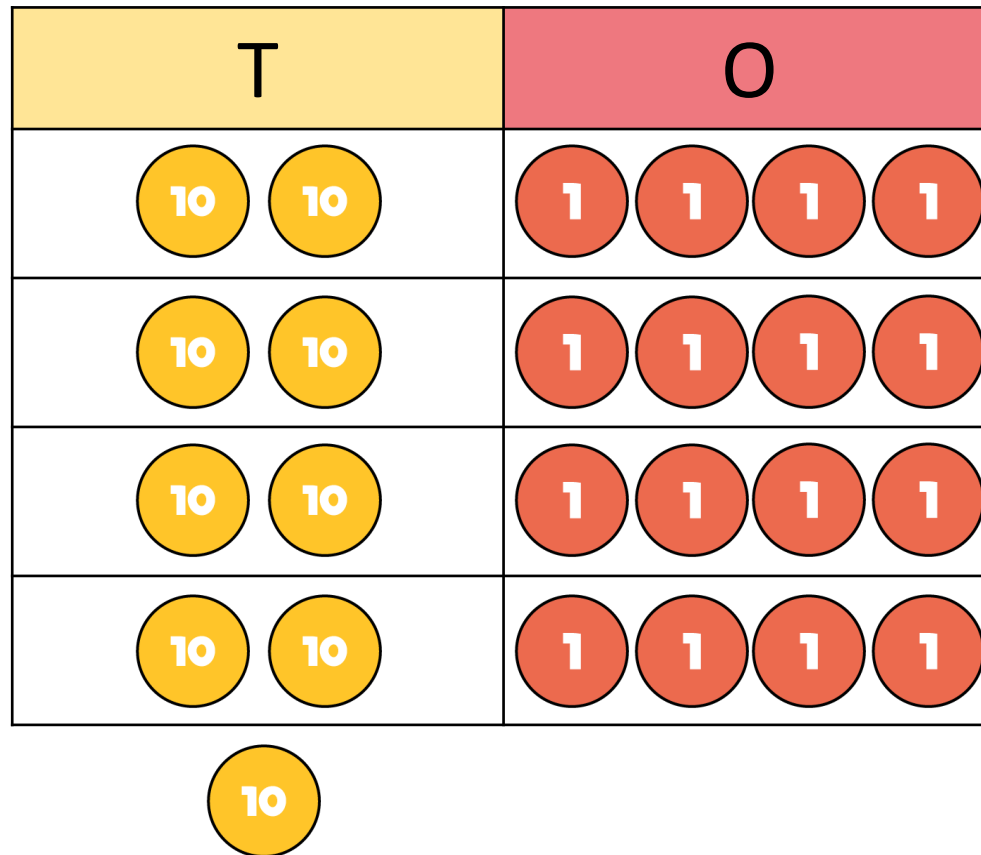
(4 × 5)
(30 × 5)





Multiplication...

$$4 \times 24 = 96$$

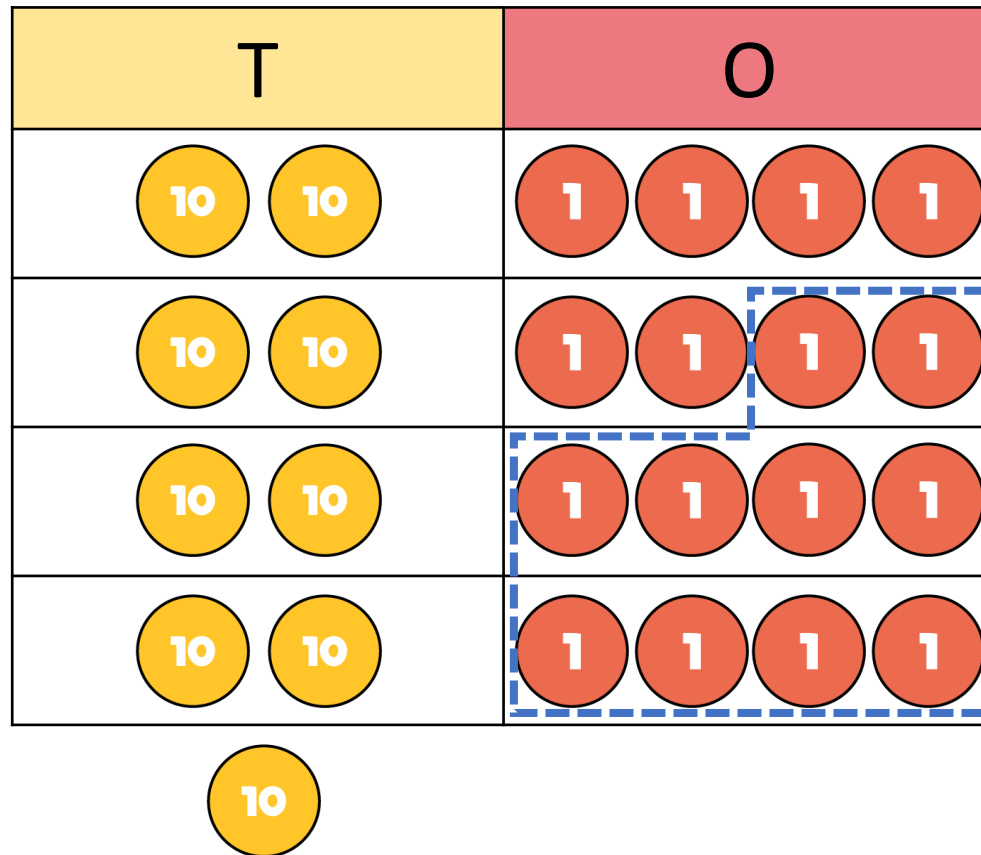


	T	O		
	2	4		
×		4		
	1	6	(4 × 4)	
	8	0	(4 × 20)	
	9	6		



Multiplication...

$$4 \times 24 = 96$$



	T	O	
	2	4	
×		4	
	9	6	
	1		



Multiplication...

	T	O		
	2	4		
×		4		
	1	6	(4 × 4)	
	8	0	(4 × 20)	
	9	6		

	T	O		
	2	4		
×		4		
	9	6		
	1			

Have a think



What is the same about each method?

What is different about each method?

Which method do you prefer? Why?



Multiplication...

×	20	3
30	600	90
1	20	3

	H	T	O	
		2	3	
×		3	1	
			3	

$$600 + 90 + 20 + 3 = 713$$



Multiplication...

×	20	3
30	600	90
1	20	3

	H	T	O	
		2	3	
×		3	1	
		2	3	

$$600 + 90 + 20 + 3 = 713$$



Multiplication...

×	20	3
30	600	90
1	20	3

	H	T	O	
		2	3	
×		3	1	
		2	3	
		9	0	

$$600 + 90 + 20 + 3 = 713$$



Multiplication...

×	20	3
30	600	90
1	20	3

	H	T	O	
		2	3	
×		3	1	
		2	3	
	6	9	0	

$$600 + 90 + 20 + 3 = 713$$



Multiplication...

×	20	3
30	600	90
1	20	3

$$600 + 90 + 20 + 3 = 713$$

	H	T	O	
		2	3	
×		3	1	
		2	3	
+	6	9	0	
	7	1	3	



Multiplication...

×	20	3
30	600	90
1	20	3

$$600 + 90 + 20 + 3 = 713$$

	H	T	O	
		2	3	
×		3	1	
<hr/>				
		2	3	
+	6	9	0	
<hr/>				
	7	1	3	

1

What is the same?

What is different?



Division...

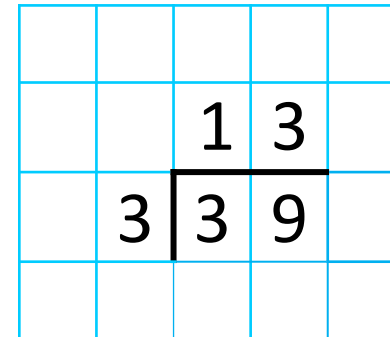
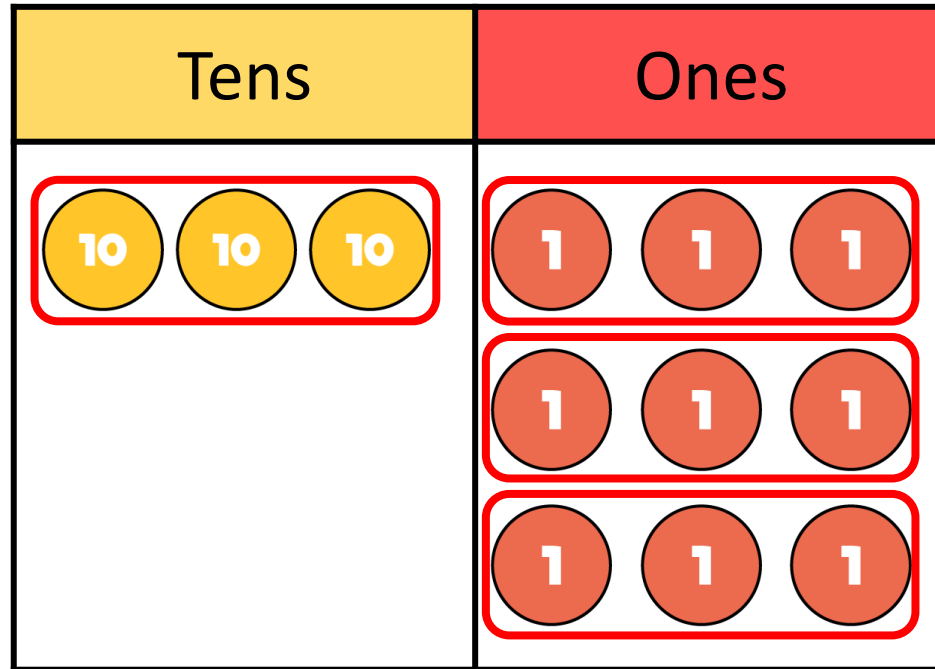
- Written method first appears in Year 5.

<p>Divide numbers up to 4 digits by a 1-digit number</p> <p>The short division method is introduced for the first time.</p>	<p>There are ... groups of ... hundreds/tens/ones/ in ... I can exchange 1 ... for 10 ...</p> <table border="1" data-bbox="937 654 1105 788"><tr><td></td><td></td><td>1</td><td>3</td></tr><tr><td>3</td><td></td><td>3</td><td>9</td></tr></table> <table border="1" data-bbox="830 811 1105 982"><thead><tr><th>T</th><th>O</th></tr></thead><tbody><tr><td>10 10 10</td><td>1 1 1</td></tr><tr><td></td><td>1 1 1</td></tr><tr><td></td><td>1 1 1</td></tr></tbody></table> <table border="1" data-bbox="1386 576 1615 705"><tr><td></td><td></td><td>2</td><td>0</td><td>5</td><td>r2</td></tr><tr><td>3</td><td></td><td>6</td><td>1</td><td>7</td><td></td></tr></table> <table border="1" data-bbox="1238 725 1615 982"><thead><tr><th>H</th><th>T</th><th>O</th></tr></thead><tbody><tr><td>100 100 100</td><td>10</td><td>1 1 1</td></tr><tr><td>100 100 100</td><td></td><td>1 1 1</td></tr><tr><td></td><td></td><td>1 1 1</td></tr></tbody></table>			1	3	3		3	9	T	O	10 10 10	1 1 1		1 1 1		1 1 1			2	0	5	r2	3		6	1	7		H	T	O	100 100 100	10	1 1 1	100 100 100		1 1 1			1 1 1	<table border="1" data-bbox="1916 545 2145 674"><tr><td></td><td></td><td></td><td>1</td><td>2</td><td>2</td><td>3</td><td>r2</td></tr><tr><td>4</td><td></td><td></td><td>4</td><td>8</td><td>9</td><td>4</td><td></td></tr></table> <table border="1" data-bbox="1773 691 2150 982"><thead><tr><th>Th</th><th>H</th><th>T</th><th>O</th></tr></thead><tbody><tr><td>1000 1000</td><td>100 100</td><td>10 10</td><td>1 1 1</td></tr><tr><td>1000 1000</td><td>100 100</td><td>10 10</td><td>1 1 1</td></tr><tr><td></td><td>100 100</td><td>10 10</td><td>1 1 1</td></tr><tr><td></td><td></td><td>10 10</td><td>1 1 1</td></tr></tbody></table>				1	2	2	3	r2	4			4	8	9	4		Th	H	T	O	1000 1000	100 100	10 10	1 1 1	1000 1000	100 100	10 10	1 1 1		100 100	10 10	1 1 1			10 10	1 1 1
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Division...

Complete the sentences.







There is 1 group of three tens.

There are 3 groups of three ones.

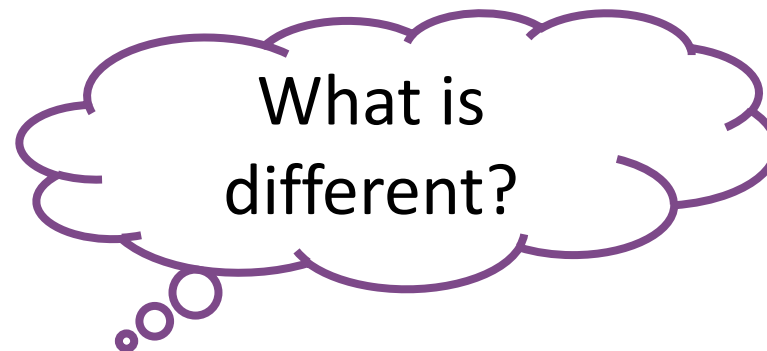
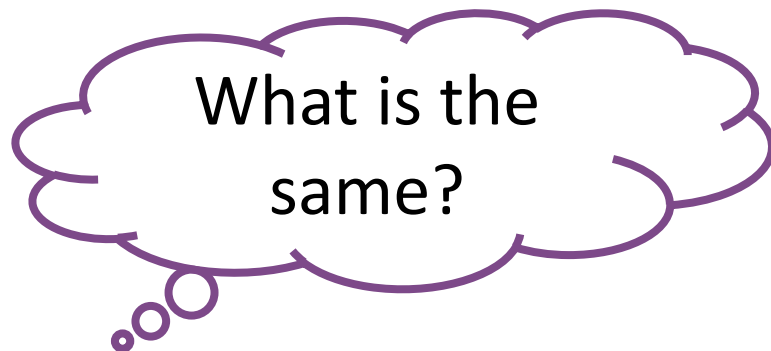
$$39 \div 3 = 13$$



Division...

Tens	Ones
	
	
	


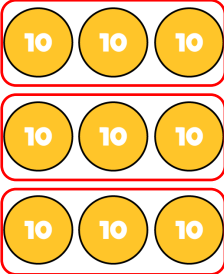
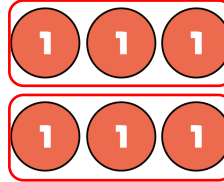
		1	3	
	3	3	9	





Division...

$$396 \div 3 =$$

H	T	O
		

		1	3	2	
	3	3	9	6	

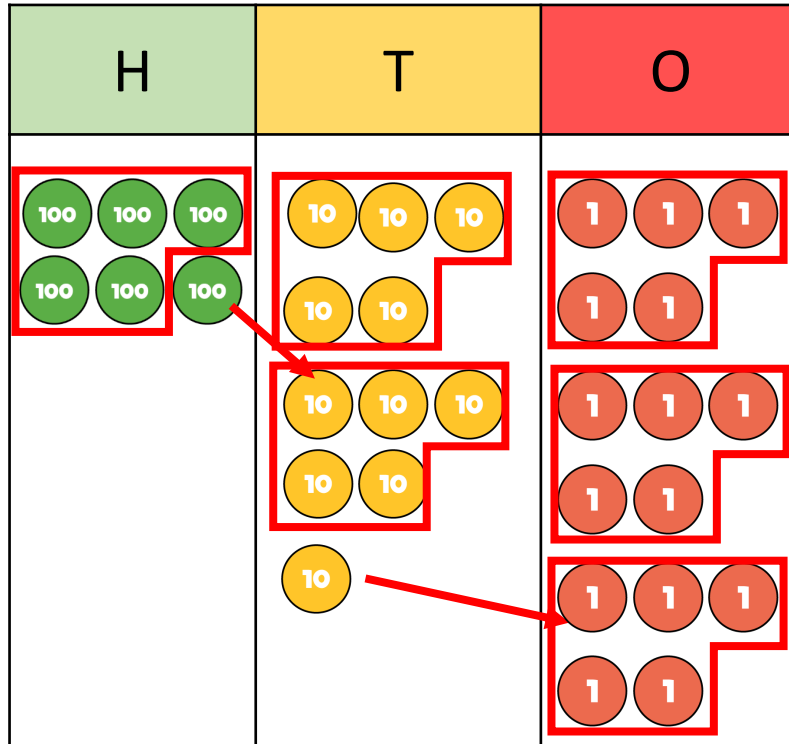
Have a think





Division...

$$615 \div 5 =$$



		1	2	3	
	5	6	1	1	5

6 hundreds divided by 5 is equal to 1
hundred with a remainder of 1
I can exchange 1 hundred for 10 tens.



Division...

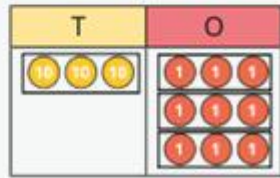
- Year 5 also introduces remainders.

Divide numbers up to 4 digits by a 1-digit number

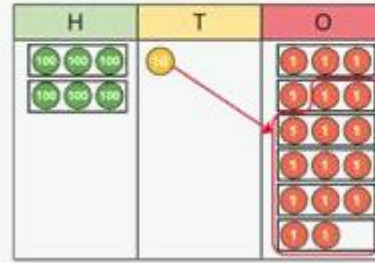
The short division method is introduced for the first time.

There are ... groups of ... hundreds/tens/ones/ in ...
I can exchange 1 ... for 10 ...

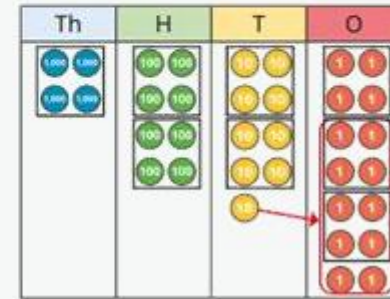
			1	3	
		3		3	9



			2	0	5
		3		6	1
					7



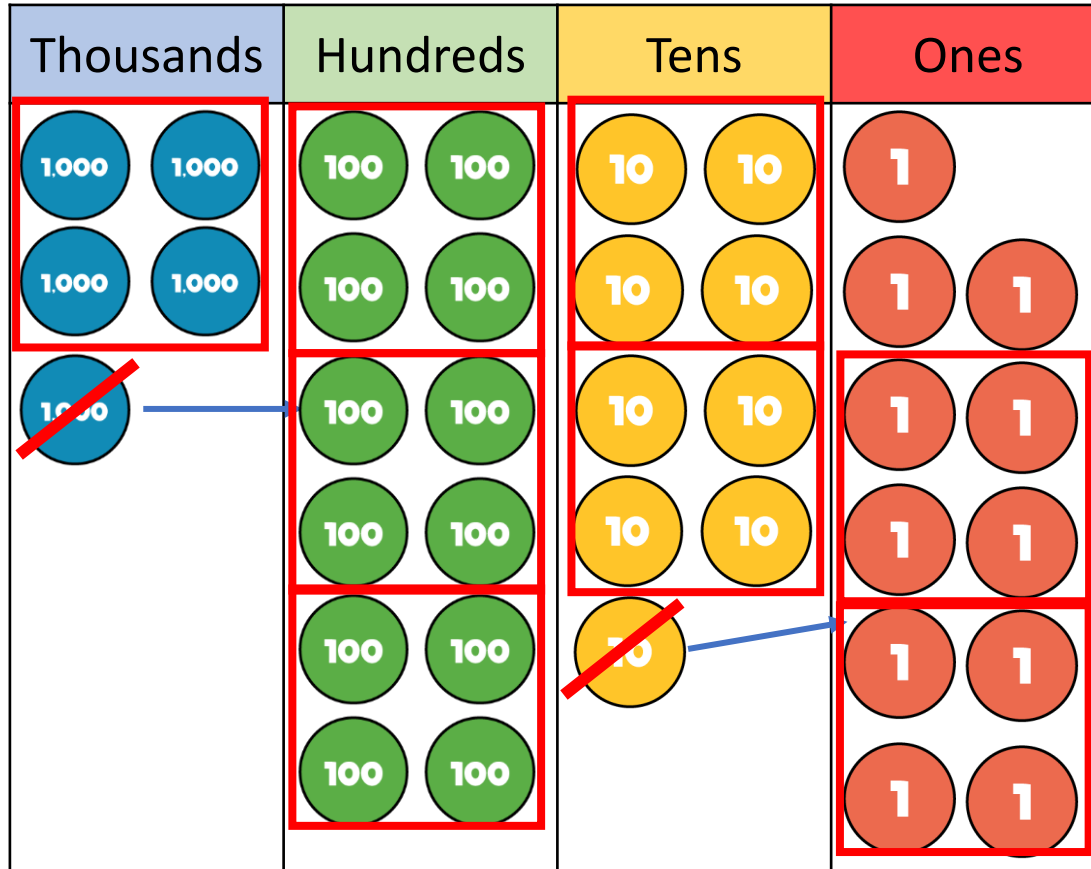
				1	2
				2	3
			4		4
					8
					9
					4





Division...

$$5,291 \div 4 = 1,322 \text{ r}3$$



		1	3	2	2	r3
4	5	¹ 2	9	¹ 1		



Division...

- Long division is introduced in Year 6.

Long division	Method 1	Method 2																																																																																																																																																																																																				
<p>The long division method is introduced for the first time. Two alternative methods are shown.</p>	<p>Method 1</p> <table border="1" data-bbox="823 615 1016 872"><tr><td></td><td></td><td></td><td></td><td></td></tr><tr><td></td><td></td><td>0</td><td>3</td><td>6</td></tr><tr><td>12</td><td></td><td>4</td><td>3</td><td>2</td></tr><tr><td></td><td></td><td>3</td><td>6</td><td>0</td></tr><tr><td></td><td></td><td>7</td><td>2</td><td></td></tr><tr><td></td><td></td><td>7</td><td>2</td><td></td></tr><tr><td></td><td></td><td></td><td></td><td>0</td></tr></table> <p>(12 × 30)</p> <table border="1" data-bbox="1136 619 1391 872"><tr><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td></tr><tr><td></td><td></td><td></td><td>0</td><td>2</td><td>4</td><td>r</td><td>12</td><td></td></tr><tr><td></td><td></td><td>15</td><td></td><td>3</td><td>7</td><td>2</td><td></td><td></td></tr><tr><td></td><td></td><td></td><td></td><td>3</td><td>0</td><td>0</td><td></td><td></td></tr><tr><td></td><td></td><td></td><td></td><td>7</td><td>2</td><td></td><td></td><td></td></tr><tr><td></td><td></td><td></td><td></td><td>6</td><td>0</td><td></td><td></td><td></td></tr><tr><td></td><td></td><td></td><td></td><td>1</td><td>2</td><td></td><td></td><td></td></tr></table> <p>(15 × 20)</p> <p>(15 × 4)</p>								0	3	6	12		4	3	2			3	6	0			7	2				7	2						0													0	2	4	r	12				15		3	7	2							3	0	0							7	2								6	0								1	2				<p>Method 2</p> <table border="1" data-bbox="1620 615 1814 872"><tr><td></td><td></td><td></td><td></td><td></td></tr><tr><td></td><td></td><td>0</td><td>3</td><td>6</td></tr><tr><td>12</td><td></td><td>4</td><td>3</td><td>2</td></tr><tr><td></td><td></td><td>3</td><td>6</td><td></td></tr><tr><td></td><td></td><td>7</td><td>2</td><td></td></tr><tr><td></td><td></td><td>7</td><td>2</td><td></td></tr><tr><td></td><td></td><td></td><td></td><td>0</td></tr></table> <table border="1" data-bbox="1918 615 2173 872"><tr><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td></tr><tr><td></td><td></td><td></td><td>0</td><td>1</td><td>0</td><td>9</td><td>r</td><td>9</td></tr><tr><td></td><td></td><td>13</td><td></td><td>1</td><td>4</td><td>2</td><td>6</td><td></td></tr><tr><td></td><td></td><td></td><td></td><td>1</td><td>3</td><td>0</td><td></td><td></td></tr><tr><td></td><td></td><td></td><td></td><td>1</td><td>2</td><td>6</td><td></td><td></td></tr><tr><td></td><td></td><td></td><td></td><td>1</td><td>1</td><td>7</td><td></td><td></td></tr><tr><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td>9</td></tr></table>								0	3	6	12		4	3	2			3	6				7	2				7	2						0													0	1	0	9	r	9			13		1	4	2	6						1	3	0							1	2	6							1	1	7											9
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Division...

Calculate:

$$598 \div 13 = 46$$

		4	6
13	<u>5</u>	9	8
—	5	2	0
		<u>7</u>	8
—		7	8
			0

$13 \times 1 = 13$

$13 \times 2 = 26$

$13 \times 3 = 39$

$13 \times 4 = 52$

$13 \times 5 = 65$

$13 \times 6 = 78$

$13 \times 7 = 91$

($\times 40$)

($\times 6$)

$13 \times 10 = 130$

$13 \times 20 = 260$

$13 \times 30 = 390$

$13 \times 40 = 520$

$13 \times 50 = 650$

$13 \times 60 = 780$

$13 \times 70 = 910$



Division...

Calculate $598 \div 13 = 46$

13	26	39	<u>52</u>	65	<u>78</u>	91	104	117	130
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		4	6
13	<u>5</u>	<u>9</u>	8
—	5	2	↓
		<u>7</u>	8
—		7	8
			0

59 tens divided by 13 is equal to 4 tens with a remainder of 7 tens.

The remainder is exchanged into 70 ones.

78 ones divided by 13 is equal to 6 ones.




National Curriculum Tests...


- What are the expectations in the tests at the end of Year 6?



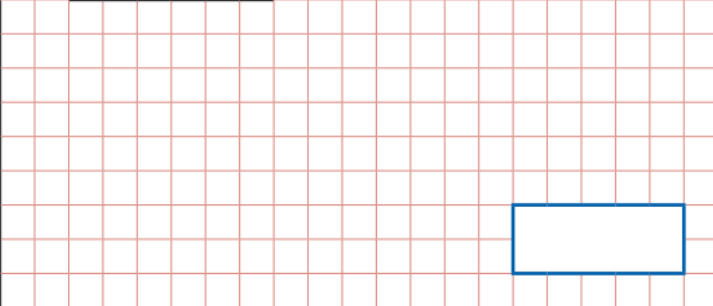
National Curriculum Tests...

- Arithmetic multiplication questions

9	$213 \times 0 =$	<input type="text"/>	<input type="checkbox"/> 1 mark
			

23	$\begin{array}{r} 836 \\ \times 27 \\ \hline \end{array}$	<input type="text"/>	<input type="checkbox"/> 2 marks
	Show your method 		

5	$9 \times 41 =$	<input type="text"/>	<input type="checkbox"/> 1 mark
			

30	$\begin{array}{r} 3468 \\ \times 62 \\ \hline \end{array}$	<input type="text"/>	<input type="checkbox"/> 2 marks
	Show your method 		



National Curriculum Tests...

- Arithmetic division questions

8	$120 \div 12 =$	<input type="checkbox"/> 1 mark
<input style="width: 100px; height: 20px;" type="text"/>		

25	$37 \overline{)888}$	<input type="checkbox"/> 2 marks
Show your method	<input style="width: 100px; height: 20px;" type="text"/>	

36	$83 \overline{)8051}$	<input type="checkbox"/> 2 marks
Show your method	<input style="width: 100px; height: 20px;" type="text"/>	



National Curriculum Tests...

- Reasoning questions

8

Ken is playing a game. He has 4,289 points.

Then he scores another 355 points.

Ken's target is 6,000 points.

How many **more** points does Ken need to reach his target?

Show
your
method

7

This picture shows the masses of eight kittens.



305 g



375 g



310 g



255 g



275 g



410 g



360 g



345 g

What is the **difference** in mass between the heaviest kitten and the lightest kitten?

 g

1 mark



National Curriculum Tests...

- Reasoning questions

9

Jack chose a number.

He multiplied the number by 7

Then he added 85

His answer was 953

What number did Jack choose?

Show
your
method

2 marks

19

A machine pours 250 millilitres of juice every 4 seconds.

How many **litres** of juice does the machine pour every **minute**?

Show
your
method



Where can you find more help?

- White Rose Maths [videos](#) for home learning.